

# Computer Science II

## Environmental Engineering Second Level 2024-2025 1<sup>st</sup> Course

## Lecture #5

# Programming with MATLAB (Cont.)

## 13. MATRICES (Cont.)

### Entering a matrix:

A matrix is an array of numbers. To type a matrix into MATLAB you must

- begin with a square bracket, [
- separate elements in a row with spaces or commas (,)
- use a semicolon (;) to separate rows
- end the matrix with another square bracket, ].

## 13. MATRICES (Cont.)

### Entering a matrix (Cont.):

Ex: This technique work for two-dimensional matrices as well

```
>> k=[ 8 9 10, 1 2 20, 4 3 30]
```

```
k= 8  9 10
```

```
    1  2 20
```

```
    4  3 30
```

Note that the use of semicolons (;) here is different from their use mentioned earlier to suppress output or to write multiple commands in a single line.

## 13. MATRICES (Cont.)

### Entering a matrix (Cont.):

Once we have entered the matrix, it is automatically stored and remembered in the Workspace. We can refer to it simply as matrix k. We can then view a particular element in a matrix by specifying its location. We write:

```
>> k(end, end) → ans = 30
```

```
>> k(2, end-1:end) → ans = 2 20
```

```
>> k(2,1) → ans = 1
```

k(2,1) is an element located in the second row and first column. Its value is 1.

## 13. MATRICES (Cont.)

### Matrix indexing:

We select elements in a matrix just as we did for vectors, but now we need two indices. The element of row  $i$  and column  $j$  of the matrix  $k$  is denoted by  $k(i,j)$ . Thus,  $k(i,j)$  in MATLAB refers to the element  $k_{ij}$  of matrix  $k$ . The first index is the row number and the second index is the column number. For example,  $k(1,3)$  is an element of first row and third column. Here,  $k(1,3)=10$ .

## 13. MATRICES (Cont.)

### Matrix indexing (Cont.):

Correcting any entry is easy through indexing. Here we substitute  $k(3, 3) = 30$  by

$k(3, 3) = 0$ . The result is:

```
>> k(3, 3) = 0
```

```
k= 8  9 10
```

```
  1  2 20
```

```
  4  3  0
```

## 13. MATRICES (Cont.)

### Deleting rows or columns:

To delete a row or column of a matrix, use the empty vector operator, [ ].

Ex: delete the second column

```
>> a = [1 2 3, 4 5 6, 7 8 9]
```

```
a = 1 2 3
```

```
4 5 6
```

```
7 8 9
```

```
>> a(:, 2) = [] → a = 1 3
```

```
4 6
```

```
7 9
```



## 13. MATRICES (Cont.)

### Deleting rows or columns (Cont.):

Ex: delete the second row

```
>> a(2, :) = [ ]
```

```
a = 1  2  3  
    7  8  9
```

Second row of matrix A is now deleted. To restore the third row, we use a technique for creating a matrix:

```
>> a = [ a(1, :); [4 5 6]; a(3,:) ]
```

## 13. MATRICES (Cont.)

### Dimension:

To determine the dimensions of a matrix or vector, use the command **size**. For example,

```
>> size(A)
```

```
ans =
```

```
    3    3
```

means 3 rows and 3 columns.

Or more explicitly with,

```
>> [m, n] = size(A)
```

## 13. MATRICES (Cont.)

### Continuation:

If it is not possible to type the entire input on the same line, use consecutive periods, called an ellipsis ..., to signal continuation, then continue the input on the next line.

```
B = [ 4/5      7.23*tan(x)    sqrt(6); ...  
      1/x^2      0          3/(x*log(x)); ...  
      x-7      sqrt(3)      x*sin(x) ];
```

Note that blank spaces around +, -, = signs are optional, but they improve readability.

## 13. MATRICES (Cont.)

### Transposing a matrix:

The transpose operation is denoted by an apostrophe or a single quote ('). It flips a matrix about its main diagonal and it turns a row vector into a column

vector. Thus,  $\gg A' \rightarrow \text{ans} = \begin{matrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 0 \end{matrix}$

By using linear algebra notation, the transpose of  $m \times n$  real matrix  $A$  is the  $n \times m$  matrix that results from interchanging the rows and columns of  $A$ . The transpose matrix is denoted  $A^T$ .

## 13. MATRICES (Cont.)

### Concatenating matrices:

Matrices can be made up of sub-matrices. Here is an example. First, let's recall our previous matrix A.

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

The new matrix B will be,

$$\gg B = [A \quad 10*A; -A \quad [1 \ 0 \ 0; 0 \ 1 \ 0; 0 \ 0 \ 1]]$$

## 13. MATRICES (Cont.)

### Concatenating matrices (Cont.):

```
>> B = [A 10*A ; -A [1 0 0 ; 0 1 0 ; 0 0 1] ]
```

```
B = 1  2  3 10 20 30  
     4  5  6 40 50 60  
     7  8  9 70 80 90  
    -1 -2 -3  1  0  0  
    -4 -5 -6  0  1  0  
    -7 -8 -9  0  0  1
```

## 13. MATRICES (Cont.)

### Matrix generators:

MATLAB provides functions that generate elementary matrices.

Elementary matrices	
<code>eye(m,n)</code>	Returns an m-by-n matrix with 1 on the main diagonal
<code>eye(n)</code>	Returns an n-by-n square identity matrix
<code>zeros(m,n)</code>	Returns an m-by-n matrix of zeros
<code>ones(m,n)</code>	Returns an m-by-n matrix of ones
<code>diag(A)</code>	Extracts the diagonal of matrix A
<code>rand(m,n)</code>	Returns an m-by-n matrix of random numbers

For a complete list of elementary matrices and matrix manipulations, type **help elmat** or **doc elmat**.

## 13. MATRICES (Cont.)

**Matrix generators (Cont.):** Here are some examples:

1. `>> b = ones (3, 1)`

`b = 1`

`1`

`1`

Equivalently, we can define b as `>> b=[1;1;1]`

2. `>> eye (3)`

`ans = 1 0 0`

`0 1 0`

`0 0 1`



## 13. MATRICES (Cont.)

### Matrix generators (Cont.):

3. `>> c = zeros (2, 3)`

`c = 0 0 0`

`0 0 0`

4. `>> C = [1 2; 3 4];`

`>> D = [C zeros (2); ones (2) eye (2)]`

`D = 1 2 0 0`

`3 4 0 0`

`1 1 1 0`

`1 1 0 1`

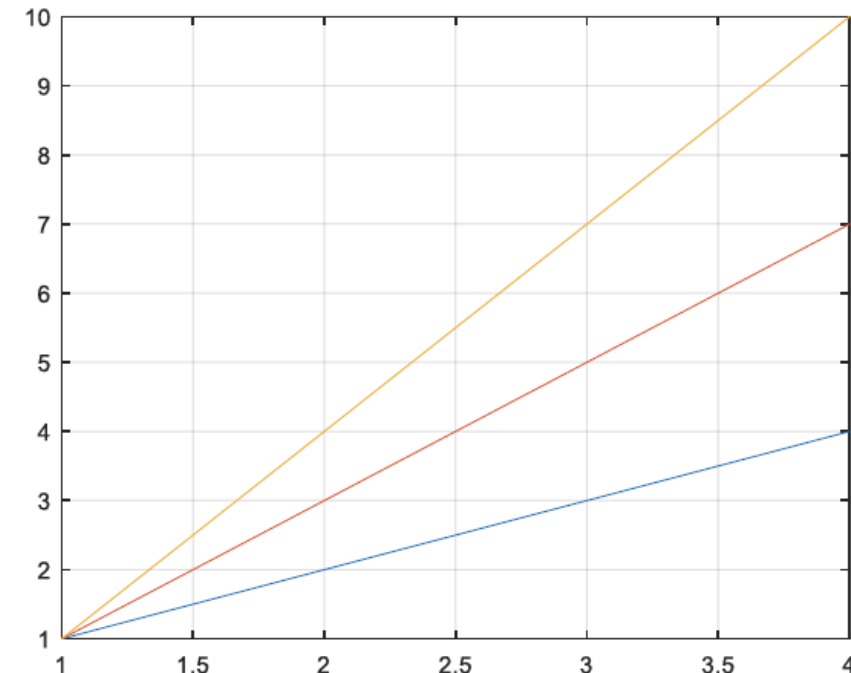
## 13. MATRICES (Cont.)

### Plotting Matrices:

If one of the arguments of the plot command is a matrix, MATLAB will use the columns of the matrix to plot a set of lines, one line per column.

```
Ex:- >> q= [ 1 1 1; 2 3 4; 3 5 7; 4 7 10]  
>> plot (q)  
>> grid
```

MATLAB plots the columns of the matrix  $q$  against the row index.



## 13. MATRICES (Cont.)

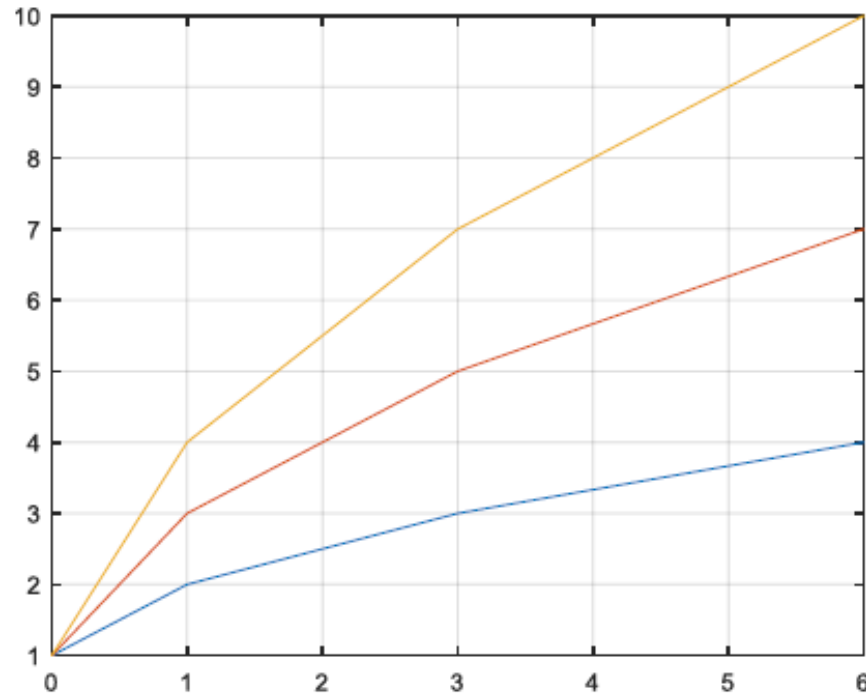
### Plotting Matrices (Cont.):

You can also supply an x variable:

```
>> x = [ 0  1  3  6];
```

```
>> plot (x, q) ;
```

```
>> grid
```

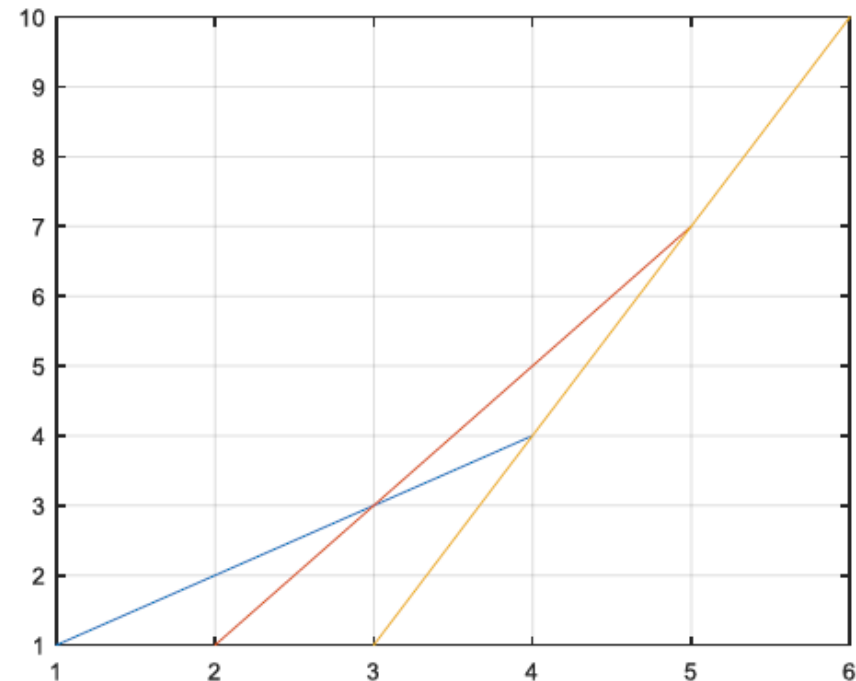


## 13. MATRICES (Cont.)

### Plotting Matrices (Cont.):

If both the x and y arguments are matrices, MATLAB will plot the successive columns on the same plot.

```
Ex:- >> q = [ 1 1 1; 2 3 4; 3 5 7; 4 7 10]
      >> x = [ 1 2 3; 2 3 4; 3 4 5; 4 5 6]
      >> plot ( x, q )
      >> grid
```



## 13. MATRICES (Cont.)

### Subplots:

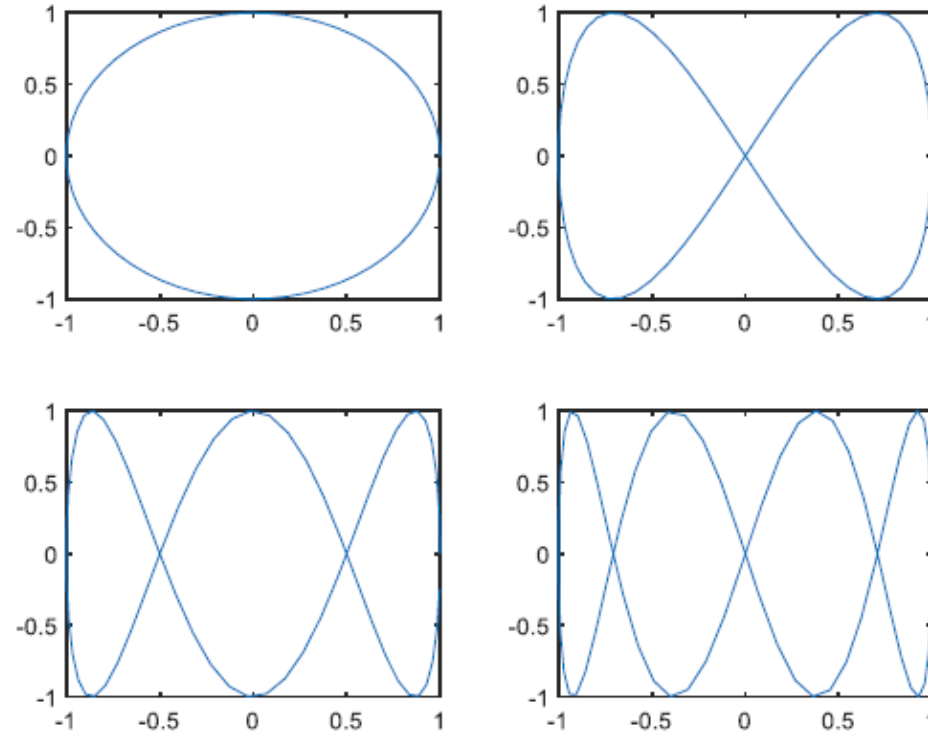
To plot more than one set of axes in the same window, use the subplot command. You can type subplot (m, n, p) ,to break up the plotting window into m plots in the vertical direction and n plots in the horizontal direction, choosing the pth plot for drawing into.

The subplots are counted as you read text: left to right along the top row, then left to right along the second row, and so on.

## 13. MATRICES (Cont.)

### Subplots (Cont.):

Ex:- `>> t= 0 : 0.1 : 2*pi;`  
`>> subplot (2, 2, 1)`  
`>> plot (cos(t), sin(t))`  
`>> subplot (2, 2, 2)`  
`>> plot (cos(t), sin(2*t))`  
`>> subplot(2, 2, 3)`  
`>> plot(cos(t), sin(3*t))`  
`>> subplot (2, 2, 4)`  
`>> plot (cos(t), sin (4*t))`



## 13. MATRICES (Cont.)

### Subplots (Cont.):

As long as your subplots are based on an array of  $9 \times 9$  little plots or less, subplot (2 2 1) or subplot 2 2 1 are equivalent to subplot (2,2,1). You can mix different subplot arrays on the same figure, as long as the plots do not overlap.

Ex:- `>> subplot 221`

`>> plot (1:10)`

`>> subplot 222`

`>> plot (0,'*')`

`>> subplot 212`

`>> plot ([1 0 1 0])`

